

Class 1 | 1.1.08 | Powers with rational exponents

Task 1. Calculate:

$$(a) 324^{0.5} =$$

$$(b) 0.0625^{0.25} =$$

$$(c) 1000^{1\frac{1}{3}} =$$

$$(d) (0.01)^{-\frac{3}{2}} =$$

$$(e) 1024^{0.3} =$$

$$(f) 64^{-\frac{2}{3}} =$$

$$(g) \left(\frac{9}{4}\right)^{-\frac{1}{2}} =$$

$$(h) \left(\frac{8}{27}\right)^{-\frac{1}{3}} =$$

Task 2. Calculate.

$$(a) \left(5^{\frac{1}{3}} \times 5^{-\frac{1}{2}} \div 5^{\frac{5}{6}}\right)^{-1} =$$

$$(b) \left(6^{-0.9} \div 6^{-\frac{4}{5}} \times 6^{1.7}\right)^{\frac{5}{8}} =$$

$$(c) \left(5^{\frac{1}{3}} \times 25^{-\frac{1}{2}} \div 0.2^{\frac{5}{6}}\right)^{-6} =$$

$$(d) \left(0.25^{-0.9} \div 2^{-\frac{4}{5}} \times 8^{1.1} \times 2^{0.1}\right)^{0.5} =$$

$$(e) \left[5^{\frac{1}{4}} \times (0.2)^{-\frac{3}{4}}\right]^{-3} =$$

$$(f) \left\{ \left(11^{\frac{1}{3}}\right)^2 \div 11^{-\frac{1}{3}} \times \frac{1}{11} \right\}^{20} \div 100^{0.5} =$$

Task 3. Convert each of the following expressions to a power with integer base and rational exponent:

$$(a) \sqrt{125\sqrt{25\sqrt{5}}} =$$

$$(b) \sqrt{8\sqrt{4 \times \sqrt[3]{2}}} =$$

$$(c) \sqrt[3]{\sqrt[5]{\sqrt[4]{7}}} = 7^{\frac{1}{60}}$$

$$(d) \sqrt{7^3} \times \sqrt[3]{\sqrt{7}} =$$

$$(e) 3\sqrt{3} \times \sqrt[3]{3} \times \sqrt[4]{3} = 3^{2\frac{1}{12}}$$

$$(f) \sqrt[5]{2^{11}} \div 2^3 \times \sqrt{2} =$$

Task 4. Compare the two given numbers without using a calculator.

$$(a) \sqrt{5 + \sqrt{10}} \text{ and } \sqrt{8}$$

$$(b) \sqrt[3]{\sqrt{10}} \quad \text{and} \quad 0.1^{-0.5} \div 10^{\frac{1}{3}}$$